

INTERMEDIATE ALGEBRA (ALGEBRA II)

TRANSFER MATH READINESS SAMPLE CHALLENGE QUESTIONS

Download the complete Study Packet:
<http://www.glendale.edu/studypackets>

Students who have taken 2 years of high school algebra or its equivalent with grades of “C” or better are eligible to take this challenge. There are a total of 45 questions. Students are allowed 45 minutes. No calculators are allowed. Sample questions from each of the eight areas below are on the back of this sheet.

Students who receive a satisfactory score may enroll in the following courses:

Math 133/111—Finite Mathematics

Math 112—Calculus for

Math 135—Liberal Arts Mathematics

Business Math 136—Statistics

Math 138—Math for Elementary Teachers

Math 110A—Pre-calculus I

Math 100—College Algebra

Math 110—Pre-calculus

The following topics are covered by the challenge:

1. Elementary Numeric & Algebraic Operations
2. Rational Expressions
3. Exponents and Radicals
4. Linear Equations; Inequalities; Absolute Value
5. Polynomials; Quadratic Equations
6. The Co-ordinate Plane & Graphing
7. Functions and Logarithms
8. Word Problems

Typical questions from each of the competency areas of the Transfer Math Readiness Challenge

1. Elementary numeric algebraic operations.

$$\frac{c}{d} + 2 =$$

- (A) $\frac{c+2d}{d}$ (B) $\frac{c+2}{d+2}$ (C) $\frac{c+2}{d}$ (D) $c+2d$ (E) c
-

2. Rational Expressions

$$\frac{c-d}{\frac{1}{d} - \frac{1}{c}} =$$

- (A) $\frac{c-d}{dc}$ (B) $\frac{dc}{c-d}$ (C) dc (D) $-dc$ (E) $\frac{1}{dc}$
-

3. Exponents and Radicals

$$\sqrt{3} + \sqrt{27}$$

- (A) 6 (B) $3\sqrt{3}$ (C) $4\sqrt{3}$ (D) $10\sqrt{3}$ (E) $\sqrt{30}$
-

4. Linear Equations; inequalities; absolute values.

If $3x + 2y = 8$ and $y = x - 1$, then $x =$

- (A) -6 (B) $\frac{6}{5}$ (C) $\frac{7}{5}$ (D) $\frac{9}{5}$ (E) 2
-

5. Polynomials; quadratic equations.

One of the roots of $(x-2)(3x+4) = 0$ is

- (A) -2 (B) $-\frac{4}{3}$ (C) $-\frac{3}{4}$ (D) $\frac{3}{4}$ (E) $\frac{4}{3}$
-

6. The coordinate plane and graphing.

Which of the following is an equation of a line with slope 3 and y-intercept -4 ?

- (A) $y = \frac{1}{3}x - 4$ (B) $y = 3x - 4$ (C) $y = 3x + 4$
(D) $y = 4x - 3$ (E) $y = 4x + 3$
-

7. Functions and logarithms.

If $\log_{10} x + \log_{10} y = 3$, then $xy =$

- (A) 0.001 (B) 1.0 (C) 10 (D) 100 (E) 1,000
-

8. Word Problems

A student who correctly answered 72 questions on a test received a score of 75%. How many questions were on the test?

- (A) 54 (B) 72 (C) 75 (D) 96 (E) 104

Practice Problems for Transfer Math Readiness Questions – Topic 1: Elementary Operations

Directions: Study the examples, work the problems, then check your answers on the back of this sheet. If you don't get the answer given, check your work and look for mistakes. If you have trouble, ask a math teacher or someone else who understands this topic.

A. Algebraic Operations, Grouping, Evaluation:
to evaluate an expression, first do powers, then multiply and divide in order from left to right, and finally add and subtract in order from left to right. Parentheses have preference.:

Example:
 1) $14 - 3^2 = 14 - 9 = 5$
 2) $2 \cdot 4 + 3 \cdot 5 = 8 + 15 = 23$
 3) $10 - 2 \cdot 3^2 = 10 - 2 \cdot 9 = 10 - 18 = -9$
 4) $(10 - 2) \cdot 3^2 = 8 \cdot 9 = 72$

1 to 7: Find the value:

- | | |
|----------------------------|---------------|
| 1. $2^3 =$ | 5. $0^4 =$ |
| 2. $-2^4 =$ | 6. $(-2^4) =$ |
| 3. $4 + 2 \cdot 5 =$ | 7. $1^5 =$ |
| 4. $3^2 - 2 \cdot 3 + 1 =$ | |

8 to 13: If $a = -3$, $b = 2$, $c = 0$, $d = 1$, and $e = -3$:

8. $a - e =$
 9. $e^2 + (d - ab)c =$
 10. $a - (bc - d) + e =$
 11. $\frac{e}{d} + \frac{b}{a} - \frac{2d}{e} =$
 12. $\frac{b}{e} =$
 13. $\frac{d}{c} =$

Combine like terms when possible:

Example:
 1) $3x + y^2 - (x + 2y^2) = 3x - x + y^2 - xy^2 = 2x - y^2$
 2) $a - a^2 + a = 2a - a^2$

14 to 20: Simplify:

14. $6x + 3 - x - 7 =$
 15. $2(3 - t) =$
 16. $10r - 5(2r - 3y) =$
 17. $x^2 - (x - x^2) =$
 18. $3a - 2(4(a - 2b) - 3a) =$
 19. $3(a + b) - 2(a - b) =$
 20. $1 + x - 2x + 3x - 4x =$

B. Simplifying Fractional Expressions:

Example:
 1) $\frac{27}{36} = \frac{9 \cdot 3}{9 \cdot 4} = \frac{9}{9} \cdot \frac{3}{4} = 1 \cdot \frac{3}{4} = \frac{3}{4}$
 (note that you must be able to find a common factor—in this case 9—in both the top and bottom in order to reduce a fraction.)
 2) $\frac{3a}{12ab} = \frac{3a \cdot 1}{3a \cdot 4b} = \frac{3a}{3a} \cdot \frac{1}{4b} = 1 \cdot \frac{1}{4b} = \frac{1}{4b}$
 (common factor: 3a)

21 to 32: Reduce:

- | | |
|-----------------------------|--|
| 21. $\frac{13}{52} =$ | 27. $\frac{5a + b}{5a + c} =$ |
| 22. $\frac{26}{65} =$ | 28. $\frac{x - 4}{4 - x} =$ |
| 23. $\frac{3 + 6}{3 + 9} =$ | 29. $\frac{2(x + 4)(x - 5)}{(x - 5)(x - 4)} =$ |
| 24. $\frac{6axy}{15by} =$ | 30. $\frac{x^2 - 9x}{x - 9} =$ |
| 25. $\frac{19a^2}{95a} =$ | 31. $\frac{8(x - 1)^2}{6(x^2 - 1)} =$ |
| 26. $\frac{14x - 7y}{7y} =$ | 32. $\frac{2x^2 - x - 1}{x^2 - 2x + 1} =$ |

Example: $\frac{3}{x} \cdot \frac{y}{15} \cdot \frac{10x}{y^2} = \frac{3 \cdot 10 \cdot x \cdot y}{15 \cdot x \cdot y^2} = \frac{3 \cdot 5 \cdot 2 \cdot x \cdot y \cdot 1}{3 \cdot 5 \cdot 1 \cdot x \cdot y \cdot y} = 1 \cdot 1 \cdot 2 \cdot 1 \cdot 1 \cdot \frac{1}{y} = \frac{2}{y}$

33 to 34: Simplify:

- | | |
|--|--|
| 33. $\frac{4x}{6} \cdot \frac{xy}{y^2} \cdot \frac{3y}{2} =$ | 34. $\frac{x^2 - 3x}{x - 4} \cdot \frac{x(x - 4)}{2x - 6} =$ |
|--|--|

B. Evaluation of Fractions

I. $a^b \cdot a^c = a^{b+c}$	IV. $(ab)^c = a^c \cdot b^c$	VII. $a^{-b} = \frac{1}{a^b}$
II. $\frac{a^b}{a^c} = a^{b-c}$	V. $\left(\frac{a}{b}\right)^c = \frac{a^c}{b^c}$	
III. $(a^b)^c = a^{bc}$	VI. $a^0 = 1$ (if $a \neq 0$)	

35 to 44: Find x:

- | | |
|------------------------------|---------------------------------------|
| 35. $2^3 \cdot 2^4 = 2^x$ | 40. $8 = 2^x$ |
| 36. $\frac{2^3}{2^4} = 2^x$ | 41. $a^x = a^3 \cdot a$ |
| 37. $3^{-4} = \frac{1}{3^x}$ | 42. $\frac{b^{10}}{b^5} = b^x$ |
| 38. $\frac{5^2}{5^2} = 2^x$ | 43. $\frac{1}{c^{-4}} = e^x$ |
| 39. $(2^4)^3 = 2^x$ | 44. $\frac{a^{3y-2}}{a^{2y-3}} = a^x$ |

Practice Problems for Transfer Math Readiness Questions – Topic 1: Elementary Operations

45 to 59: *Simplify:*

- | | |
|---------------------------------|------------------------------------|
| 45. $8x^0 =$ | 53. $2^{c+3} \cdot 2^{c-3} =$ |
| 46. $3^{-4} =$ | 54. $\frac{8x}{2^{x-1}} =$ |
| 47. $2^3 \cdot 2^3 =$ | 55. $\frac{2x^{-3}}{6x^{-4}} =$ |
| 48. $0^5 =$ | 56. $(a^{x+3})^x =$ |
| 49. $5^0 =$ | 57. $\frac{a^{3x-2}}{a^{2x-3}} =$ |
| 50. $(-3)^3 - 3^3 =$ | 58. $(-2a^2)^4(ab^2) =$ |
| 51. $2^x \cdot 4^{x-1} =$ | 59. $2(4xy^2)^{-1}(-2x^{-1}y)^2 =$ |
| 52. $\frac{2^{c+3}}{2^{c-3}} =$ | |

C. Scientific Notation

Examples:

- $32800 = 3.2800 \times 10^4$ if the zeros in the ten's and one's places are significant. If the one's zero is not, write 3.280×10^4 , if neither is significant: 3.28×10^4
- $0.004031 = 4.031 \times 10^{-3}$
- $2 \times 10^2 = 200$
- $9.9 \times 10^{-1} = 0.99$

Note that scientific form always looks like $a \times 10^n$ where $1 \leq a < 10$, and n is an integer power of 10.

60 to 63: *Write in scientific notation:*

- | | |
|--------------------|--------------|
| 60. $93,000,000 =$ | 62. $5.07 =$ |
| 61. $0.000042 =$ | 63. $-32 =$ |

64 to 66: *Write in standard notation:*

- | | |
|------------------------------|--------------------------|
| 64. $1.4030 \times 10^3 =$ | 66. $4 \times 10^{-6} =$ |
| 65. $-9.11 \times 10^{-2} =$ | |

To compute with numbers written in scientific form, separate the parts, compute, then recombine.

Examples:

- $(3.14 \times 10^5)(2) =$
 $(3.14)(2) \times 10^5 = 6.28 \times 10^5$
- $\frac{4.28 \times 10^6}{2.14 \times 10^{-2}} = \frac{4.28}{2.14} \times \frac{10^6}{10^{-2}} = 2.00 \times 10^8$
- $\frac{2.01 \times 10^{-3}}{8.04 \times 10^{-6}} = 0.250 \times 10^3 = 2.50 \times 10^2$

67 to 74: *Write answer in scientific notation:*

- | | |
|--|---|
| 67. $10^{40} \times 10^{-2} =$ | 71. $\frac{1.8 \times 10^{-8}}{3.6 \times 10^{-5}} =$ |
| 68. $\frac{10^{-40}}{10^{-10}} =$ | 72. $(4 \times 10^{-3})^2 =$ |
| 69. $\frac{1.86 \times 10^4}{3 \times 10^{-1}} =$ | 73. $(2.5 \times 10^2)^{-1} =$ |
| 70. $\frac{3.6 \times 10^{-5}}{1.8 \times 10^{-8}} =$ | |
| 74. $\frac{(-2.92 \times 10^3)(4.1 \times 10^7)}{-8.2 \times 10^{-3}} =$ | |

E. Absolute value:

Example:

- $|3| = 3$
- $|-3| = 3$
- $|a|$ depends on 'a':
if $a \geq 0$, $|a| = a$; if $a < 0$, $|a| = -a$
- $-|-3| = -3$

75 to 78: *Find the value:*

- | | |
|-----------------------|--------------------|
| 75. $ 0 =$ | 77. $ 3 + -3 =$ |
| 76. $\frac{ a }{a} =$ | 78. $ 3 - -3 =$ |

79 to 84: *If $x = -4$, find:*

- | | |
|-----------------|--------------------------------------|
| 79. $ x + 1 =$ | 82. $x + x =$ |
| 80. $ 1 - x =$ | 83. $ -3x =$ |
| 81. $- x =$ | 84. $\left x - (x - x) \right =$ |

Answers:

- | | | |
|-------------------------|-----------------------------|---|
| 1. 8 | 29. $\frac{2(x+4)}{x-4}$ | 57. a^{x+1} |
| 2. -16 | 30. x | 58. $16a^9b^2$ |
| 3. 14 | 31. $\frac{4(x-1)}{3(x+1)}$ | 59. $2/x^3$ |
| 4. 4 | 32. $\frac{2x+1}{x-1}$ | 60. 9.3×10^7 |
| 5. 0 | 33. x^2 | 61. 4.2×10^{-5} |
| 6. 16 | 34. $x^2/2$ | 62. 5.07 |
| 7. 1 | 35. 7 | 63. -3.2×10 |
| 8. 0 | 36. -1 | 64. 1403.0 |
| 9. 9 | 37. 4 | 65. -0.0911 |
| 10. -5 | 38. 0 | 66. 0.000004 |
| 11. -3 | 39. 12 | 67. 1.0×10^{38} |
| 12. -2/3 | 40. 3 | 68. 1.0×10^{-30} |
| 13. no value | 41. 4 | 69. 6.2×10^4 |
| 14. $5x - 4$ | 42. 5 | 70. 2.0×10^3 |
| 15. $6 - 2t$ | 43. 4 | 71. 5.0×10^{-4} |
| 16. $15y$ | 44. $y + 1$ | 72. 1.6×10^{-5} |
| 17. $2x^2 - x$ | 45. 8 | 73. 4.0×10^{-3} |
| 18. $a + 16b$ | 46. 1/81 | 74. 1.46×10^{13} |
| 19. $a + 5b$ | 47. 128 | 75. 0 |
| 20. $1 - 2x$ | 48. 0 | 76. 1 if $a > 0$
-1 if $a < 0$
(no value if $a = 0$) |
| 21. 1/4 | 49. 1 | 77. 6 |
| 22. 2/5 | 50. -54 | 78. 0 |
| 23. 3/4 | 51. 2^{3x-2} | 79. 3 |
| 24. $\frac{2ax}{5b}$ | 52. 64 | 80. 5 |
| 25. $a/5$ | 53. 2^{2c} | 81. -4 |
| 26. $\frac{2x-y}{5a+b}$ | 54. 2^{2x+1} | 82. 0 |
| 27. $\frac{5a+b}{5a+c}$ | 55. $x/3$ | 83. 12 |
| 28. -1 | 56. a^{x^2+3x} | 84. 12 |

Practice Problems for Transfer Math Readiness Questions – Topic 2: Rational Expressions

Directions: Study the examples, work the problems, then check your answers on the back of this sheet. If you don't get the answer given, check your work and look for mistakes. If you have trouble, ask a math teacher or someone else who understands this topic.

A. Adding and Subtracting Fractions:
if denominators are the same, combine the numerators:

$$\text{Example: } \frac{3x}{y} - \frac{x}{y} = \frac{3x - y}{y} = \frac{2x}{y}$$

1 to 5: Find the sum or difference as indicated (reduce if possible):

1. $\frac{4}{7} + \frac{2}{7} =$
2. $\frac{3}{x-3} - \frac{x}{x-3} =$
3. $\frac{b-a}{b+a} - \frac{a-b}{b+a} =$
4. $\frac{x+2}{x^2+2x} - \frac{3y^2}{xy^2} =$
5. $\frac{3a}{b} + \frac{2}{b} - \frac{a}{b} =$

If denominators are different, find equivalent fractions with common denominators:

Examples:

- 1) $\frac{3}{4}$ is the equivalent to how many eighths?
 $\frac{3}{4} = \frac{?}{8}$ $\frac{3}{4} = 1 \cdot \frac{3}{4} = \frac{2}{2} \cdot \frac{3}{4} = \frac{2 \cdot 3}{2 \cdot 4} = \frac{6}{8}$
- 2) $\frac{6}{5a} = \frac{?}{5ab}$ $\frac{6}{5a} = \frac{b}{b} \cdot \frac{6}{5a} = \frac{6b}{5ab}$
- 3) $\frac{3x+2}{x+1} = \frac{?}{4(x+1)}$
 $\frac{3x+2}{x+1} = \frac{4}{4} \cdot \frac{3x+2}{x+1} = \frac{12x+8}{4x+4}$
- 4) $\frac{x-1}{x+1} = \frac{?}{(x+1)(x-2)}$
 $\frac{x-1}{x+1} = \frac{(x-2)(x-1)}{(x-2)(x+1)} = \frac{x^2 - 3x + 2}{(x-2)(x+1)}$

6 to 10: Complete:

6. $\frac{4}{9} = \frac{?}{72}$
7. $\frac{3x}{7} = \frac{?}{7y}$
8. $\frac{x+3}{x+2} = \frac{?}{(x-1)(x+2)}$
9. $\frac{30-15a}{15-15b} = \frac{?}{(1+b)(1-b)}$
10. $\frac{x-6}{6-x} = \frac{?}{-2}$

How to get the lowest common denominator (LCD) by finding the least common multiple (LCM) of all denominators.

Examples:

- 1) $\frac{5}{6}$ and $\frac{8}{15}$: First find the LCM of 6 and 15:
 $6 = 2 \cdot 3$ $15 = 3 \cdot 5$
LCM = $2 \cdot 3 \cdot 5 = 30$, so $\frac{5}{6} = \frac{25}{30}$, and $\frac{8}{15} = \frac{16}{30}$
- 2) $\frac{3}{4}$ and $\frac{1}{6a}$:
 $4 = 2 \cdot 2$ $6a = 2 \cdot 3 \cdot a$
LCM = $2 \cdot 2 \cdot 3 \cdot a = 12a$, so
 $\frac{3}{4} = \frac{9a}{12a}$, and $\frac{1}{6a} = \frac{2}{12a}$
- 3) $\frac{2}{3(x+2)}$ and $\frac{ax}{6(x+1)}$
so: $\frac{2}{3(x+2)} = \frac{2 \cdot 2(x+1)}{2 \cdot 3(x+1)(x+2)} = \frac{4(x+1)}{6(x+1)(x+2)}$
and $\frac{ax}{6(x+1)} = \frac{ax(x+2)}{6(x+1)(x+2)}$

11 to 16: Find equivalent fractions with the lowest common denominator:

11. $\frac{2}{3}$ and $\frac{2}{9}$
12. $\frac{3}{x}$ and 5
13. $\frac{x}{3}$ and $\frac{-4}{x+1}$
14. $\frac{3}{x-2}$ and $\frac{4}{2-x}$
15. $\frac{x}{15(x^2-2)}$ and $\frac{7x(y-1)}{10(x-1)}$
16. $\frac{1}{x}$, $\frac{3x}{x+1}$ and $\frac{x^2}{x^2+x}$

After finding equivalent fractions with common denominators, proceed as before (combine numerators):

Examples:

- 1) $\frac{a}{2} - \frac{a}{4} = \frac{2a}{4} - \frac{a}{4} = \frac{2a-a}{4} = \frac{a}{4}$
- 2) $\frac{3}{x-1} + \frac{1}{x+2} = \frac{3(x+2)}{(x-1)(x+2)} + \frac{(x-1)}{(x-1)(x+2)}$
 $= \frac{3x+6+x-1}{(x-1)(x+2)} = \frac{4x+5}{(x-1)(x+2)}$

17 to 30: Find the sum or difference

17. $\frac{3}{a} - \frac{1}{2a} =$
18. $\frac{3}{x} - \frac{2}{a} =$
19. $\frac{4}{5} - \frac{2}{x} =$
20. $\frac{2}{5} + 2 =$
21. $\frac{a}{b} - 2 =$
22. $a - \frac{c}{b} =$
23. $\frac{1}{a} + \frac{1}{b} =$
24. $a - \frac{1}{a} =$
25. $\frac{x}{x-1} - \frac{x}{1-x} =$
26. $\frac{3x-2}{x-2} - \frac{2}{x+2} =$
27. $\frac{2x-1}{x+1} - \frac{2x-1}{x-2} =$
28. $\frac{1}{(x-1)(x-2)} + \frac{1}{(x-2)(x-3)}$
 $= \frac{2}{(x-3)(x-1)} =$
29. $\frac{x}{x-2} - \frac{4}{x^2-2x} =$
30. $\frac{x}{x-2} - \frac{4}{x^2-4} =$

Practice Problems for Transfer Math Readiness Questions – Topic 2: Rational Expressions

B. Multiplying Fractions: Multiply the tops, multiply the bottoms, reduce if possible:

Examples:

1) $\frac{3}{4} \cdot \frac{2}{5} = \frac{6}{20} = \frac{3}{10}$

2) $\frac{3(x+1)}{x-2} \cdot \frac{x^2-4}{x^2-1} = \frac{3(x+1)(x+2)(x-2)}{(x-2)(x+1)(x-1)} = \frac{3x+6}{x-1}$

31 to 38: *Multiply, reduce if possible*

<p>31. $\frac{2}{3} \cdot \frac{3}{8} =$</p> <p>32. $\frac{a}{b} \cdot \frac{c}{d} =$</p> <p>33. $\frac{2}{7a} \cdot \frac{ab}{12} =$</p> <p>34. $\frac{3(x+4)}{5y} \cdot \frac{5y^3}{x^2-16} =$</p>	<p>35. $\frac{(a+b)^3}{(x-y)^2} \cdot \frac{x-y}{5-p} \cdot \frac{(p-5)^2}{(a+b)^2} =$</p> <p>36. $\left(\frac{3}{4}\right)^2 =$</p> <p>37. $\left(\frac{2a^3}{5b}\right)^3 =$</p> <p>38. $\left(2\frac{1}{2}\right)^2 =$</p>
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C. Dividing Fractions: A nice way to do this is to make a compound fraction and then multiply the top and bottom (of the big fraction) by the LCD of both:

Examples:

1) $\frac{a}{b} \div \frac{c}{d} = \frac{\frac{a}{b}}{\frac{c}{d}} = \frac{a}{b} \cdot \frac{bd}{c} = \frac{ad}{bc}$

2) $\frac{7}{\frac{2}{3} - \frac{1}{2}} = \frac{7 \cdot 6}{\left(\frac{2}{3} - \frac{1}{2}\right) \cdot 6} = \frac{42}{\frac{4}{6} - \frac{3}{6}} = \frac{42}{\frac{1}{6}} = 42$

3) $\frac{5x}{2y} \div 2x = \frac{\frac{5x}{2y}}{2x} = \frac{5x}{2y} \cdot \frac{1}{2x} = \frac{5x}{4xy} = \frac{5}{4y}$

39 to 53: *Simplify:*

<p>39. $\frac{3}{4} \div \frac{2}{3} =$</p> <p>40. $11\frac{3}{8} \div \frac{3}{4} =$</p> <p>41. $\frac{3}{4} \div 2 =$</p> <p>42. $\frac{a}{b} \div 3 =$</p> <p>43. $\frac{3}{a} \div \frac{b}{3} =$</p> <p>44. $\frac{\frac{x+7}{x^2-9}}{1} =$</p> <p>45. $\frac{\frac{a-4}{3} - 2}{a} =$</p> <p>46. $\frac{2a-b}{\frac{1}{2}} =$</p>	<p>47. $\frac{2}{3/4} =$</p> <p>48. $\frac{2/3}{4} =$</p> <p>49. $\frac{a/b}{c} =$</p> <p>50. $\frac{a}{b/c} =$</p> <p>51. $\frac{\frac{1}{a} - \frac{1}{b}}{\frac{1}{a} + \frac{1}{b}} =$</p> <p>52. $\frac{\frac{1}{2a} - \frac{1}{b}}{\frac{1}{a} - \frac{1}{2b}} =$</p> <p>53. $\frac{\frac{1}{a} - \frac{1}{b}}{\frac{1}{ab}} =$</p>
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Answers:

<p>1. $\frac{6}{7}$</p> <p>2. -1</p> <p>3. $\frac{2b-2a}{b+a}$</p> <p>4. $-\frac{2}{x}$</p> <p>5. $\frac{2a+2}{b}$</p> <p>6. 32</p> <p>7. $3xy$</p> <p>8. x^2+2x-3</p> <p>9. $2+2b-a-ab$</p> <p>10. 2</p> <p>11. $\frac{6}{9}, \frac{2}{9}$</p> <p>12. $\frac{3}{x}, \frac{5x}{x}$</p> <p>13. $\frac{x(x+1)}{3(x+1)}, \frac{-12}{3(x+1)}$</p> <p>14. $\frac{3}{x-2}, \frac{-4}{x-2}$</p> <p>15. $\frac{2x(x-1)}{30(x^2-2)(x-1)}, \frac{21x(y-1)(x^2-2)}{30(x^2-2)(x-1)}$</p> <p>16. $\frac{x+1}{x(x+1)}, \frac{3x^2}{x(x+1)}, \frac{x^2}{x(x+1)}$</p> <p>17. $\frac{5}{2a}$</p> <p>18. $\frac{3a-2x}{ax}$</p> <p>19. $\frac{4x-10}{5x}$</p> <p>20. $12/5$</p> <p>21. $\frac{a-2b}{b}$</p> <p>22. $\frac{ab-c}{b}$</p> <p>23. $\frac{a+b}{ab}$</p> <p>24. $\frac{a^2-1}{a}$</p> <p>25. 0</p> <p>26. $\frac{3x^2-2x}{x^2-4}$</p> <p>27. $\frac{-3(2x-1)}{(x+1)(x-2)}$</p> <p>28. 0</p> <p>29. $\frac{x+2}{x}$</p> <p>30. $\frac{x^2+2x-4}{x^2-4}$</p> <p>31. $1/4$</p>	<p>32. $\frac{ac}{bd}$</p> <p>33. $\frac{b}{42}$</p> <p>34. $\frac{3y^2}{x-4}$</p> <p>35. $\frac{(a+b)(5-p)}{x-y}$</p> <p>36. $\frac{9}{16}$</p> <p>37. $\frac{8a^9}{125b^3}$</p> <p>38. $25/4$</p> <p>39. $9/8$</p> <p>40. $91/6$</p> <p>41. $3/8$</p> <p>42. $\frac{a}{3b}$</p> <p>43. $\frac{9}{ab}$</p> <p>44. $\frac{x+7}{x+3}$</p> <p>45. $\frac{a^2-4a}{3-2a}$</p> <p>46. $4a-2b$</p> <p>47. $8/3$</p> <p>48. $\frac{1}{6}$</p> <p>49. $\frac{a}{bc}$</p> <p>50. $\frac{ac}{b}$</p> <p>51. $\frac{b-a}{b+a}$</p> <p>52. $\frac{b-2a}{2b-a}$</p> <p>53. $b-a$</p>
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Practice Problems for Transfer Math Readiness Questions – Topic 3: Exponents and Radicals

Directions: Study the examples, work the problems, then check your answers on the back of this sheet. If you don't get the answer given, check your work and look for mistakes. If you have trouble, ask a math teacher or someone else who understands this topic.

A. Definitions of Powers and Roots:

1 to 20: Find the value.

1. $2^3 =$
2. $3^2 =$
3. $-4^2 =$
4. $(-4)^2 =$
5. $0^4 =$
6. $1^4 =$
7. $\sqrt{64} =$
8. $\sqrt[3]{64} =$
9. $\sqrt[6]{64} =$
10. $-\sqrt{49} =$
11. $\sqrt[3]{-125} =$
12. $\sqrt{5^2} =$
13. $\sqrt{(-5)^2} =$
14. $\sqrt{a^2} =$
15. $\sqrt[3]{a^3} =$
16. $\sqrt{\frac{1}{4}} =$
17. $\sqrt{0.04} =$
18. $\left(\frac{2}{3}\right)^4 =$
19. $\sqrt[4]{81a^8} =$
20. $\sqrt{7} \cdot \sqrt{7} =$

B. Laws of Integer Exponents

I. $a^b \cdot a^c = a^{b+c}$	IV. $(ab)^c = a^c \cdot b^c$
II. $\frac{a^b}{a^c} = a^{b-c}$	V. $\left(\frac{a}{b}\right)^c = \frac{a^c}{b^c}$
III. $(a^b)^c = a^{bc}$	VI. $a^0 = 1$ (if $a \neq 0$)
VII. $a^{-b} = \frac{1}{a^b}$	

21 to 30: Find x:

21. $2^3 \cdot 2^4 = 2^x$
22. $\frac{2^3}{2^4} = 2^x$
23. $3^{-4} = \frac{1}{3^x}$
24. $\frac{5^2}{5^2} = 5^x$
25. $(2^3)^4 = 2^x$
26. $8 = 2^x$
27. $a^3 \cdot a = a^x$
28. $\frac{b^{10}}{b^5} = b^x$
29. $\frac{1}{c^{-4}} = c^x$
30. $\frac{a^{3y-2}}{a^{2y-3}} = a^x$

31 to 43: Find the value:

31. $7x^0 =$
32. $3^{-4} =$
33. $2^3 \cdot 2^4 =$
34. $0^5 =$
35. $5^0 =$
36. $(-3)^3 - 3^3 =$
37. $x^{c+3} \cdot x^{c-3} =$
38. $2^x \cdot 4^{x-1} =$
39. $\frac{x^{c+3}}{x^{c-3}} =$
40. $\frac{8^x}{2^{x-1}} =$
41. $\frac{2x^{-3}}{6x^{-4}} =$
42. $(a^x+3)^{x-3} =$
43. $\frac{a^{3x-2}}{a^{2x-3}} =$

44 to 47: Write the given two ways:

	no negative powers	no fractions
44. $\frac{d^{-4}}{d^4} =$		
45. $\left(\frac{3x^3}{y}\right)^{-2} =$		
46. $\left(\frac{a^2bc}{2ab^2c}\right)^3 =$		
47. $\frac{x^2y^3z^{-1}}{x^5y^{-6}z^{-3}} =$		

C. Laws of Rational Exponents,

Radicals: Assume all radicals are real numbers:

<p>I. If r is a positive integer, p is an integer, and $a \geq 0$, then</p> $a^{p/r} = \sqrt[r]{a^p} = \left(\sqrt[r]{a}\right)^p$ <p>which is a real number. (Also true if r is a positive odd integer and $a < 0$.)</p> <p>Think of $\frac{p}{r}$ as $\frac{\text{power}}{\text{root}}$.</p> <p>II. $\sqrt[r]{ab} = \sqrt[r]{a} \cdot \sqrt[r]{b}$, or $(ab)^{1/r} = a^{1/r} \cdot b^{1/r}$</p> <p>III. $\sqrt[r]{\frac{a}{b}} = \frac{\sqrt[r]{a}}{\sqrt[r]{b}}$, or $\left(\frac{a}{b}\right)^{1/r} = \frac{a^{1/r}}{b^{1/r}}$</p> <p>IV. $\sqrt[rs]{a} = \sqrt[r]{\sqrt[s]{a}} = \sqrt[s]{\sqrt[r]{a}}$ or $a^{1/rs} = \left(a^{1/s}\right)^{1/r} = \left(a^{1/r}\right)^{1/s}$</p>
--

48 to 53: Write as a radical:

48. $3^{1/2} =$
49. $4^{2/3} =$
50. $(1/2)^{1/3} =$
51. $x^{3/2} =$
52. $2x^{1/2} =$
53. $(2x)^{1/2} =$

54 to 57: Write as a fractional power:

54. $\sqrt{5} =$
55. $\sqrt{2^3} =$
56. $\sqrt[3]{a} =$
57. $\frac{1}{\sqrt{a}} =$

Practice Problems for Transfer Math Readiness Questions – Topic 3: Exponents and Radicals

58 to 62: Find x:

58. $\sqrt{4} \cdot \sqrt{9} = \sqrt{x}$

59. $\sqrt{x} = \frac{\sqrt{4}}{\sqrt{9}}$

60. $\sqrt[3]{64} = \sqrt{x}$

61. $\sqrt[3]{\sqrt{64}} = x$

62. $x = \frac{8^{2/3}}{4^{3/2}}$

63 to 64: Write with positive exponents:

63. $(9x^6y^{-2})^{1/2} =$

64. $(-8a^6b^{-12})^{-2/3} =$

D. Simplification of Radicals:

Examples:

1) $\sqrt{32} = \sqrt{16} \cdot \sqrt{2} = 4\sqrt{2}$

2) $\sqrt[3]{72} = \sqrt[3]{8} \cdot \sqrt[3]{9} = 2\sqrt[3]{9}$

3) $\sqrt[3]{54} + 4\sqrt[3]{16} = \sqrt[3]{27} \cdot \sqrt[3]{2} + 4\sqrt[3]{8} \cdot \sqrt[3]{2}$
 $= 3\sqrt[3]{2} + 4 \cdot 2\sqrt[3]{2} = 3\sqrt[3]{2} + 8\sqrt[3]{2} = 11\sqrt[3]{2}$

4) $\sqrt{8} - \sqrt{2} = 2\sqrt{2} - \sqrt{2} = \sqrt{2}$

65 to 82: Simplify (assume all radicals are real numbers):

65. $-\sqrt{81} =$

66. $\sqrt{50} =$

67. $3\sqrt{12} =$

68. $\sqrt[3]{54} =$

69. $\sqrt{52} =$

70. $2\sqrt{3} + \sqrt{27} - \sqrt{75} =$

71. $\sqrt{x^5} =$

72. $\sqrt{4x^6} =$

73. $x\sqrt{2x} + 2\sqrt{2x^3} + \frac{2x^2}{\sqrt{2x}} =$

74. $\sqrt{a^2} =$

75. $\sqrt{a^3} =$

76. $\sqrt[3]{a^5} =$

77. $3\sqrt{2} + \sqrt{2} =$

78. $5\sqrt{3} - \sqrt{3} =$

79. $\sqrt{9x^2 - 9y^2} =$

80. $\sqrt{9x^2 + 9y^2} =$

81. $\sqrt{9(x+y)^2} =$

82. $\sqrt[3]{64(x+y)^3} =$

E. Rationalization of Denominators:

Examples:

1) $\frac{\sqrt{5}}{\sqrt{8}} = \frac{\sqrt{5}}{\sqrt{8}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{10}}{\sqrt{16}} = \frac{\sqrt{10}}{4}$

2) $\frac{1}{\sqrt[3]{2}} = \frac{1}{\sqrt[3]{2}} \cdot \frac{\sqrt[3]{4}}{\sqrt[3]{4}} = \frac{\sqrt[3]{4}}{\sqrt[3]{8}} = \frac{\sqrt[3]{4}}{2}$

3) $\frac{\sqrt{3}}{\sqrt{3}-1} = \frac{\sqrt{3}}{\sqrt{3}-1} \cdot \frac{\sqrt{3}+1}{\sqrt{3}+1}$
 $= \frac{\sqrt{9} + \sqrt{3}}{3-1} = \frac{3 + \sqrt{3}}{2}$

83 to 91: Simplify:

83. $\sqrt{\frac{2}{3}} =$

84. $\frac{1}{\sqrt{5}} =$

85. $\frac{3}{\sqrt{3}} =$

86. $\frac{\sqrt{a}}{\sqrt{b}} =$

87. $\sqrt[3]{\frac{2}{3}} =$

88. $\sqrt{2} + \frac{1}{\sqrt{2}} =$

89. $\frac{3}{\sqrt{2}+1} =$

90. $\frac{\sqrt{3}}{1-\sqrt{3}} =$

91. $\frac{\sqrt{3}+2}{\sqrt{3}-2} =$

Answers:

1. 8
2. 9
3. -16
4. 16
5. 0
6. 1
7. 8
8. 4
9. 2
10. -7
11. -5
12. 5
13. 5
14. x if $x \geq 0$; $-x$ if $x < 0$
15. a
16. 1/2
17. 0.2
18. 16/81
19. $3a^2$
20. 7
21. 7
22. -1

23. 4

24. 0

25. 12

26. 3

27. 4

28. 5

29. 4

30. $y + 1$

31. 7

32. 1/81

33. 128

34. 0

35. 1

36. -54

37. x^{2c}

38. 2^{3x-2}

39. x^6

40. 2^{2x+1}

41. $x/3$

42. a^{x^2-9}

43. a^{x+1}

44. $\frac{1}{d^d} = d^{-d}$

45. $\frac{y^2}{9x^6} = 9^{-1}x^{-6}y^2$

46. $\frac{a^3}{8b^3} = 8^{-1}a^3b^{-3}$

47. $\frac{y^9z^2}{x^3} = x^{-3}y^9z^2$

48. $\sqrt{3}$

49. $\sqrt[3]{16}$

50. $\sqrt[3]{\frac{1}{2}} = \frac{\sqrt[3]{4}}{2}$

51. $\sqrt{x^3} = x\sqrt{x}$

52. $2\sqrt{x}$

53. $\sqrt{2x}$

54. $5^{1/2}$

55. $2^{3/2}$

56. $a^{1/3}$

57. $a^{-1/2}$

58. 36

59. 4/9

60. 4

61. 2

62. 1/2

63. $\frac{3|x|^3}{|y|}$

64. $\frac{b^8}{4a^4}$

65. -9

66. $5\sqrt{2}$

67. $6\sqrt{3}$

68. $3\sqrt[3]{2}$

69. $2\sqrt{13}$

70. 0

71. $x^2\sqrt{x}$

72. $2|x|^3$

73. $4x\sqrt{2x}$

74. a if $a \geq 0$;

-a if $a < 0$

75. $a\sqrt{a}$

76. $a\sqrt[3]{a^2}$

77. $4\sqrt{2}$

78. $4\sqrt{3}$

79. $3\sqrt{x^2 - y^2}$

80. $3\sqrt{x^2 + y^2}$

81. $3|x + y|$

82. $4(x + y)$

83. $\frac{\sqrt{6}}{3}$

84. $\frac{\sqrt{5}}{5}$

85. $\sqrt{3}$

86. $\frac{\sqrt{ab}}{b}$

87. $\frac{\sqrt[3]{18}}{3}$

88. $\frac{3\sqrt{2}}{2}$

89. $3\sqrt{2} - 3$

90. $\frac{\sqrt{3} + 3}{-2}$

91. $-7 + 4\sqrt{3}$

Practice Problems for Transfer Math Readiness Questions – Topic 4: Linear Equations and Inequalities

Directions: Study the examples, work the problems, then check your answers on the back of this sheet. If you don't get the answer given, check your work and look for mistakes. If you have trouble, ask a math teacher or someone else who understands this topic.

A. Solving One Linear Equation in One Variable:
 Add or subtract the same thing on each side of the equation, or multiply or divide each side by the same thing, with the goal of getting the variable alone on one side. If there are one or more fractions, it may be desirable to eliminate them by multiplying both sides by the common denominator. If the equation is a proportion, you may wish to cross-multiply.

1 to 15: *Solve:*

- | | |
|------------------------------------|-------------------------------------|
| 1. $2x = 9$ | 9. $x - 4 = \frac{x}{2} + 1$ |
| 2. $3 = \frac{6x}{5}$ | 10. $\frac{3x}{2x+1} = \frac{5}{2}$ |
| 3. $3x + 7 = 6$ | 11. $6 - 4x = x$ |
| 4. $\frac{x}{3} = \frac{5}{4}$ | 12. $\frac{3x-2}{2x+1} = 4$ |
| 5. $5 - x = 9$ | 13. $\frac{x+3}{2x-1} = 2$ |
| 6. $x = \frac{2x}{5} + 1$ | 14. $7x - 5 = 2x + 10$ |
| 7. $4x - 6 = x$ | 15. $\frac{1}{3} = \frac{x}{x+8}$ |
| 8. $\frac{x-1}{x+1} = \frac{6}{7}$ | |

To solve a linear equation for one variable in terms of the other(s), do the same as above:

Examples:

- 1) Solve for F : $C = \frac{5}{9}(F - 32)$
 Multiply by $\frac{9}{5}$: $\frac{9}{5}C = F - 32$
 Add 32: $\frac{9}{5}C + 32 = F$
 Thus, $F = \frac{9}{5}C + 32$
- 2) Solve for b : $a + b = 90$
 Subtract a : $b = 90 - a$

16 to 21: *Solve for the indicated variable in terms of the other(s):*

- | | |
|------------------------------|-------------------------------------|
| 16. $a + b = 180$
$b =$ | 19. $y = 3x - 2$
$x =$ |
| 17. $2a + 2b = 180$
$b =$ | 20. $y = 4 - x$
$x =$ |
| 18. $P = 2b + 2h$
$b =$ | 21. $y = \frac{2}{3}x + 1$
$x =$ |

B. Solving a Pair of Linear Equations in Two Variables: the solution consists of an ordered pair, an infinite number of ordered pairs, or no solution.

22 to 29: *Solve for the common solution(s) by substitution or linear combinations:*

- | | |
|---|---|
| 22. $\begin{cases} x + 2y = 7 \\ 3x - y = 28 \end{cases}$ | 23. $\begin{cases} x + y = 5 \\ x - y = -3 \end{cases}$ |
|---|---|

24. $\begin{cases} 2x - y = -9 \\ x = 8 \end{cases}$

25. $\begin{cases} 2x - y = 1 \\ y = x - 5 \end{cases}$

26. $\begin{cases} 2x - 3y = 5 \\ 3x + 5y = 1 \end{cases}$

27. $\begin{cases} 4x - 1 = y \\ 4x + y = 1 \end{cases}$

28. $\begin{cases} x + y = 3 \\ x + y = 1 \end{cases}$

29. $\begin{cases} 2x - y = 3 \\ 6x - 9 = 3y \end{cases}$

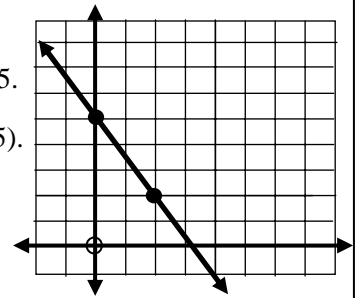
C. Analytic Geometry of One Linear Equation in Two Variables:

The graph of $y = mx + b$ is a line with slope m and y-intercept b . To draw the graph, find one point on it (such as $(0, b)$) and then use the slope to find another point. Draw the line joining the two.

Example: $y = \frac{-3}{2}x + 5$

has slope $-\frac{3}{2}$ and y-intercept 5.

To graph the line, locate $(0, 5)$. From that point, go down 3 (top of slope fraction), and over (right) 2 (bottom of fraction) to find a second point. Join.



30 to 34: *Find slope and y-intercept, and sketch the graph:*

30. $y = x + 4$
 31. $y = -\frac{1}{2}x - 3$
 32. $2y = 4x - 8$
 33. $x - y = -1$
 34. $x = -3y + 2$

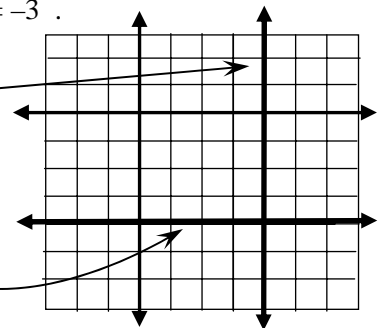
A vertical line has no slope, and its equation can be written so it looks like $x = k$ (where k is a number). A horizontal line has zero slope, and its equation looks like $y = k$.

Example: Graph on the same graph:

$x - 3 = 1$ and $1 + y = -3$.

The first equation is $x = 4$.

The second is $y = -4$.



35 to 36: *Graph and write equations for:*

35. the line thru $(-1, 4)$ and $(-1, 2)$.
 36. the horizontal line thru $(4, -1)$.

Practice Problems for Transfer Math Readiness Questions—Topic 4: Linear Equations and Inequalities

D. Analytic Geometry of Two Linear Equations in Two Variables:

Two distinct lines in a plane are either parallel or intersecting. They are parallel if and only if they have the same slope, and hence the equations of the lines have no common solutions. If the lines have unequal slopes, they intersect in one point and their equations have exactly one common solution. (They are perpendicular iff their slopes are negative reciprocals, or one is horizontal and the other is vertical.) If one equation is a multiple of the other, each equation has the same graph, and every solution of one equation is the solution of the other.

37 to 44: For each pair of equations in problems 22 to 29, tell whether the lines are parallel, perpendicular, intersecting but not perpendicular, or the same line:

- | | |
|----------------|----------------|
| 37. Problem 22 | 41. Problem 26 |
| 38. 23 | 42. 27 |
| 39. 24 | 43. 28 |
| 40. 25 | 44. 29 |

E. Solution of a One-Variable Equation Reducible to a Linear Equation: Some equations which don't appear linear can be solved by using a related linear equation.

Example: $|3 - x| = 2$
 Since the absolute value of both 2 and -2 is 2, $3 - x$ can be either 2 or -2. Write these two equations and solve each:

$$\begin{array}{l} 3 - x = 2 \quad \text{or} \quad 3 - x = -2 \\ -x = -1 \quad \quad \quad -x = -5 \\ x = 1 \quad \quad \quad \underline{\text{or}} \quad x = 5 \end{array}$$

45 to 49: Solve:

- | | |
|-------------------|--------------------|
| 45. $ x = 3$ | 48. $ 2 - 3x = 0$ |
| 46. $ x = -1$ | 49. $ x + 2 = 1$ |
| 47. $ x - 1 = 3$ | |

Examples:

1) $\sqrt{2x - 1} = 5$ Square both sides: $2x - 1 = 25$
 Solve: $2x = 26$
 $x = 13$

Be sure to check answer(s):

$$\sqrt{2x - 1} = \sqrt{2 \cdot 13 - 1} = \sqrt{25} = 5 \quad (\text{check})$$

2) $\sqrt{x} = -3$
 Square: $x = 9$
 Check: $\sqrt{3} = \sqrt{9} = 3 \neq -3$

There is no solution, since 9 doesn't satisfy the original equation (it is false that $\sqrt{9} = -3$).

50 to 52: Solve and check:

50. $\sqrt{3 - x} = 4$
 51. $\sqrt{2x + 1} = \sqrt{x - 3}$
 52. $3 = \sqrt{3x - 2}$

F. Linear Inequalities:

Rules for inequalities:

If $a > b$, then:

$$\begin{array}{l} a + c > b + c \\ a - c > b - c \\ ac > bc \quad (\text{if } c > 0) \\ ac < bc \quad (\text{if } c < 0) \\ \frac{a}{c} > \frac{b}{c} \quad (\text{if } c > 0) \\ \frac{a}{c} < \frac{b}{c} \quad (\text{if } c < 0) \end{array}$$

If $a < b$, then:

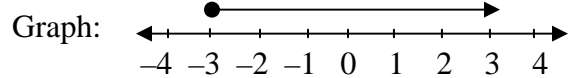
$$\begin{array}{l} a + c < b + c \\ a - c < b - c \\ ac < bc \quad (\text{if } c > 0) \\ ac > bc \quad (\text{if } c < 0) \\ \frac{a}{c} < \frac{b}{c} \quad (\text{if } c > 0) \\ \frac{a}{c} > \frac{b}{c} \quad (\text{if } c < 0) \end{array}$$

Example: One variable graph:

Solve and graph on a number line: $1 - 2x \leq 7$

(This is an abbreviation for: $\{x : 1 - 2x \leq 7\}$)

Subtract 1, get $-2x \leq 6$
 Divide by -2, $x \geq -3$



53 to 59: Solve and graph on number line:

- | | |
|---------------------|---------------------|
| 53. $x - 3 > 4$ | 57. $4 - 2x < 6$ |
| 54. $4x < 2$ | 58. $5 - x > x - 3$ |
| 55. $2x + 1 \leq 6$ | 59. $x > 1 + 4$ |
| 56. $3 < x - 3$ | |

Answers:

- | | |
|--|-----------------------------|
| 1. 9/2 | 32. $m = 2$
$b = -4$ |
| 2. 5/2 | 33. $m = 1$
$b = 1$ |
| 3. -1/3 | 34. $m = -1/3$
$b = 2/3$ |
| 4. 15/4 | 35. $x = -1$ |
| 5. -4 | 36. $y = -1$ |
| 6. 5/3 | 37. int., not \perp |
| 7. 2 | 38. \perp |
| 8. 13 | 39. int., not \perp |
| 9. 10 | 40. int., not \perp |
| 10. -5/4 | 41. int., not \perp |
| 11. 6/5 | 42. int., not \perp |
| 12. -6/5 | 43. parallel |
| 13. 5/3 | 44. same line |
| 14. 3 | 45. $\{-3, 3\}$ |
| 15. 4 | 46. no solution |
| 16. $180 - a$ | 47. $\{-2, 4\}$ |
| 17. $90 - a$ | 48. $\{2/3\}$ |
| 18. $F/2 - h$ | 49. $\{-3, -1\}$ |
| 19. $(y + 2)/3$ | 50. $\{-13\}$ |
| 20. $4 - y$ | 51. no solution |
| 21. $3(y - 1)/2$ | 52. $\{11/3\}$ |
| 22. $(9, -1)$ | 53. $x > 7$ |
| 23. $(1, 4)$ | 54. $x < 1/2$ |
| 24. $(8, 25)$ | 55. $x \leq 5/2$ |
| 25. $(-4, -9)$ | 56. $x > 6$ |
| 26. $(28/19, -13/19)$ | 57. $x > -1$ |
| 27. $(1/4, 0)$ | 58. $x < 4$ |
| 28. no solution | 59. $x > 5$ |
| 29. $(a, 2a - 3)$, where a is any number; Infinite # of solutions | |
| 30. $m = 1$
$b = 4$ | |
| 31. $m = -1/2$
$b = -3$ | |

Directions: Study the examples, work the problems, then check your answers on the back of this sheet. If you don't get the answer given, check your work and look for mistakes. If you have trouble, ask a math teacher or someone else who understands this topic.

E. Multiplying Polynomials

Examples:

- 1) $(x+2)(x+3) = x^2 + 5x + 6$
- 2) $(2x-1)(x+2) = 2x^2 + 3x - 2$
- 3) $(x-5)(x+5) = x^2 - 25$
- 4) $-4(x-3) = -4x + 12$
- 5) $(x+2)(x^2-2x+4) = x^3 + 8$
- 6) $(3x-4)^2 = (3x-4)(3x-4) = 9x^2 - 24x + 16$
- 7) $(x+3)(a-5) = ax - 5x + 3a - 15$

1 to 10: *Multiply.*

1. $(x+3)^2 =$
2. $(x-3)^2 =$
3. $(x+3)(x-3) =$
4. $(2x+3)(2x-3) =$
5. $(x-4)(x-2) =$
6. $-6x(3-x) =$
7. $(2x-1)(4x^2+2x+1) =$
8. $(x-\frac{1}{2})^2 =$
9. $(x-1)(x+3) =$
10. $(x^2-1)(x^2+3) =$

B. Factoring

Monomial Factors:

$$ab + ac = a(b + c)$$

Examples:

- 1) $x^2 - x = x(x - 1)$
- 2) $4x^2y + 6xy = 2xy(2x + 3)$

Difference of Two Squares:

$$a^2 - b^2 = (a + b)(a - b)$$

Example:

$$9x^2 - 4 = (3x + 2)(3x - 2)$$

Trinomial Square:

$$a^2 + 2ab + b^2 = (a + b)^2$$

$$a^2 - 2ab + b^2 = (a - b)^2$$

Example:

$$x^2 - 6x + 9 = (x - 3)^2$$

Trinomial:

Examples:

- 1) $x^2 - x - 2 = (x - 2)(x + 1)$
- 2) $6x^2 - 7x - 3 = (3x + 1)(2x - 3)$

Sum and Difference of Two

Cubes:

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

Example:

$$x^3 - 64 = x^3 - 4^3 = (x - 4)(x^2 + 4x + 16)$$

11 to 27: *Factor completely:*

11. $a^2 + ab =$
12. $a^3 - a^2b + ab^2 =$
13. $8x^2 - 2 =$
14. $x^2 - 10x + 25 =$
15. $-4xy + 10x^2 =$
16. $2x^2 - 3x - 5 =$
17. $x^2 - x - 6 =$
18. $x^2y - y^2x =$
19. $8x^3 + 1 =$
20. $x^2 - 3x - 10 =$
21. $2x^2 - x =$
22. $8x^3 + 8x^2 + 2x =$
23. $9x^2 + 12x + 4 =$
24. $6x^3y^2 - 9x^4y =$
25. $1 - x - 2x^2 =$
26. $3x^2 - 10x + 3 =$
27. $x^4 + 3x^2 - 4 =$

C. Solving Quadratic Equations by Factoring:

If $ab = 0$, then $a = 0$ or $b = 0$.

Example: If $(3 - x)(x + 2) = 0$ then $(3 - x) = 0$ or $(x + 2) = 0$ and thus $x = 3$ or $x = -2$

Note: there must be a zero on one side of the equation to solve by the factoring method.

Example: $6x^2 = 3x$
 Rewrite: $6x^2 - 3x = 0$
 Factor: $3x(2x - 1) = 0$
 So, $3x = 0$ or $(2x - 1) = 0$
 Thus, $x = 0$ or $x = 1/2$

28 to 39: *Solve by factoring:*

28. $x(x - 3) = 0$
29. $x^2 - 2x = 0$
30. $2x^2 = x$
31. $3x(x + 4) = 0$
32. $x^2 = 2 - x$
33. $x^2 + x = 6$

34. $(x + 2)(x - 3) = 0$

35. $(2x + 1)(3x - 2) = 0$

36. $6x^2 = x + 2$

37. $9 + x^2 = 6x$

38. $1 - x = 2x^2$

39. $x^2 - x - 6 = 0$

D. Completing the Square: $x^2 + bx$ will be the square of a binomial when c is added, if c is found as follows: find half the x coefficient and square it -- this is c .
 Thus $c = \left(\frac{b}{2}\right)^2 = \frac{b^2}{4}$, and $x^2 + bx + c = x^2 + bx + \frac{b^2}{4} = \left(x + \frac{b}{2}\right)^2$

Example: $x^2 + 5x$

Half of 5 is $5/2$, and $(5/2)^2 = 25/4$, which must be added to complete the square: $x^2 + 5x + \frac{25}{4} = \left(x + \frac{5}{2}\right)^2$

If the coefficient of x^2 is not 1, factor so it is.

Example: $3x^2 - x = 3\left(x^2 - \frac{1}{3}x\right)$

Half of $-1/3$ is $-1/6$, and $(-1/6)^2 = 1/36$, so $\left(x^2 - \frac{1}{3}x + \frac{1}{36}\right) = 3x^2 - x + \frac{3}{36}$.

Thus, $\frac{3}{36}$ or $\left(\frac{1}{12}\right)$ must be added to $3x^2 - x$ to complete the square.

40 to 43: *Complete the square, and tell what must be added:*

- | | |
|-----------------|--------------------------|
| 40. $x^2 - 10x$ | 42. $x^2 - \frac{3}{2}x$ |
| 41. $x^2 + x$ | 43. $2x^2 + 8x$ |

E. The Quadratic Formula: if a quadratic equation looks like $ax^2 + bx + c = 0$, then the roots (solutions) can be found by using the quadratic formula:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

44 to 49: *Solve*

44. $x^2 - x - 6 = 0$
45. $x^2 + 2x = -1$
46. $2x^2 - x - 2 = 0$
47. $x^2 - 3x - 4 = 0$
48. $x^2 + x - 5 = 0$
49. $x^2 + x = 1$

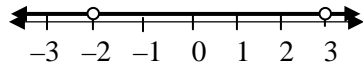
F. Quadratic Inequalities

Example: Solve $x^2 - x < 6$. First make one side zero: $x^2 - x - 6 < 0$.

Factor: $(x - 3)(x + 2) < 0$. If $(x - 3) = 0$ or $(x + 2) = 0$, then $x = 3$ or $x = -2$.

These two numbers (3 and -2) split the real numbers into three sets (visualize the number line):

x	(x - 3)	(x + 2)	(x - 3)(x + 2)	solution?
$x < -2$	negative	negative	positive	no
$-2 < x < 3$	negative	positive	negative	yes
$x > 3$	positive	positive	positive	no



Therefore, if $(x - 3)(x + 2) < 0$, then $-2 < x < 3$.

Note that this solution means that $x > -2$ and $x < 3$

50 to 54: Solve, and graph on number line:

- | | | |
|-----------------------|---------------------|------------------------|
| 50. $x^2 - x - 6 > 0$ | 52. $x^2 - 2x < -1$ | 54. $2x^2 + x - 1 > 0$ |
| 51. $x^2 + 2x < 0$ | 53. $x > x^2$ | |

G. Complex Numbers: $\sqrt{-1}$ is defined to be i , so $i^2 = -1$.

Example: $i^3 = i^2 \cdot i = -1 \cdot i = -i$

55. Find the value of i^4 .

A complex number is of the form $a + bi$, where a and b are real numbers. "a" is called the real part and "b" is the imaginary part. If "b" is zero, $a + bi$ is a real number. If $a = 0$, then $a + bi$ is pure imaginary.

Complex number operations:

Examples:

- $(3 + i) + (2 - 3i) = 5 - 2i$
- $(3 + i) - (2 - 3i) = 1 + 4i$
- $(3 + i)(2 - 3i) = 6 - 7i - 3i^2 = 6 - 7i + 3 = 9 - 7i$
- $\frac{3 + i}{2 - 3i} = \frac{3 + i}{2 - 3i} \cdot \frac{2 + 3i}{2 + 3i} = \frac{6 + 11i - 3}{4 + 9} = \frac{3 + 11i}{13} = \frac{3}{13} + \frac{11}{13}i$

56 to 65. Write each of the following so the answer is in the form $a + bi$.

- | | |
|--------------------------------|---------------------|
| 56. $(3 + 2i)(3 - 2i)$ | 63. $i^8 =$ |
| 57. $(3 + 2i) + (3 - 2i) =$ | 64. $i^{1991} =$ |
| 58. $(3 + 2i) - (3 - 2i) =$ | 65. $\frac{1}{i} =$ |
| 59. $(3 + 2i) \div (3 - 2i) =$ | |
| 60. $i^5 =$ | |
| 61. $i^6 =$ | |
| 62. $i^7 =$ | |

66 to 67: Solve and write the answer as $a + bi$.

66. $x^2 + 2x + 5 = 0$
 67. $x^2 + x + 2 = 0$

Answers:

- $x^2 + 6x + 9$
- $x^2 - 6x + 9$
- $x^2 - 9$
- $4x^2 - 9$
- $x^2 - 6x + 8$
- $-18x + 6x^2$
- $8x^3 - 1$
- $x^2 - x + 1/4$
- $x^2 + 2x - 3$
- $x^4 + 2x^2 - 3$
- $a(a + b)$
- $a(a^2 - ab + b^2)$
- $2(2x + 1)(2x - 1)$
- $(x - 5)^2$
- $2x(-2y + 5x)$
- $(2x - 5)(x + 1)$
- $(x - 3)(x + 2)$
- $xy(x - y)$
- $(2x + 1)(4x^2 - 2x + 1)$
- $(x - 5)(x + 2)$
- $x(2x - 1)$
- $2x(2x + 1)^2$
- $(3x + 2)^2$
- $3x^3y(2y - 3x)$
- $(1 - 2x)(1 + x)$
- $(3x - 1)(x - 3)$
- $(x^2 + 4)(x + 1)(x - 1)$
- $\{0, 3\}$
- $\{0, 2\}$
- $\{0, 1/2\}$
- $\{-4, 0\}$

- $\{-2, 1\}$
- $\{-3, 2\}$
- $\{-2, 3\}$
- $\{-1/2, 2/3\}$
- $\{-1/2, 2/3\}$
- $\{3\}$
- $\{-1, 1/2\}$
- $\{-2, 3\}$
- $(x - 5)^2$, add 25
- $(x + 1/2)^2$, add $1/4$
- $(x - 3/4)^2$, add $9/16$
- $2(x + 2)^2$, add 8
- $\{-2, 3\}$
- $\{-1\}$

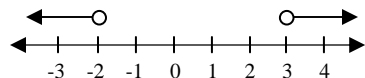
46. $\left\{ \frac{1 \pm \sqrt{17}}{2} \right\}$

47. $\{-1, 4\}$

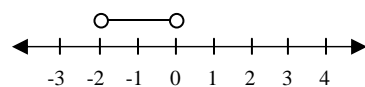
48. $\left\{ \frac{-1 \pm \sqrt{21}}{2} \right\}$

49. $\left\{ \frac{-1 \pm \sqrt{5}}{2} \right\}$

50. $x < -2$ or $x > 3$

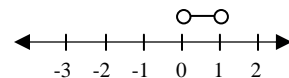


51. $-2 < x < 0$

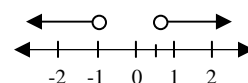


52. no solution – no graph

53. $0 < x < 1$



54. $x < -1$ or $x > 1/2$



55. 1

56. 13

57. 6

58. 4i

59. $\frac{5}{13} + \frac{12}{13}i$

60. i

61. -1

62. -i

63. 1

64. -i

65. -i

66. $-1 \pm 2i$

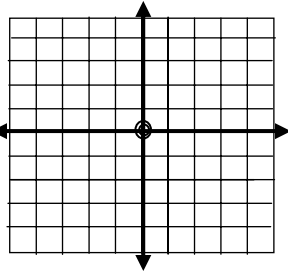
67. $-\frac{1}{2} \pm \frac{\sqrt{7}}{2}i$

Practice Problems for Transfer Math Readiness Questions– Topic 6: Graphing and the Coordinate Plane

Directions: Study the examples, work the problems, then check your answers on the back of this sheet. If you don't get the answer given, check your work and look for mistakes. If you have trouble, ask a math teacher or someone else who understands this topic.

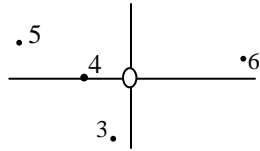
A. Graphing Points:

1. Join the following points in the given order: $(-3, -2)$, $(1, -4)$, $(3, 0)$, $(2, 3)$, $(-1, 2)$, $(3, 0)$, $(-3, -2)$, $(-1, 2)$, $(1, -4)$



2. In what quadrant does the point (a, b) lie, if $a > 0$ and $b < 0$?

3 to 6: For each given point, which of its coordinates, x or y , is larger?



B. Distance between points: the distance between the points $P_1(x_1, y_1)$ and $P_2(x_2, y_2)$ is found by using the Pythagorean Theorem, which gives $P_1P_2 = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$.

Example: $A(3, -1)$, $B(-2, 4)$

$$AB = \sqrt{(4 - (-1))^2 + (-2 - 3)^2}$$

$$= \sqrt{5^2 + (-5)^2} = \sqrt{50} = \sqrt{25 \cdot 2} = 5\sqrt{2}$$

7 to 10: Find the length of the segment joining the given points:

7. $(4, 0)$, $(0, -3)$
 8. $(-1, 2)$, $(-1, 5)$
 9. $(2, -4)$, $(0, 1)$
 10. $(-\sqrt{3}, -5)$, $(3\sqrt{3}, -6)$

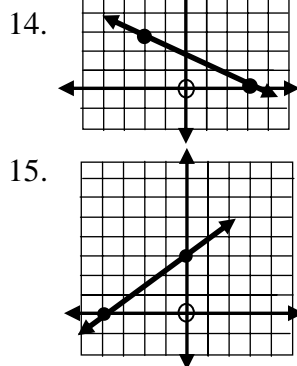
C. Linear Equations in Two Variables, Slope, Intercepts, and Graphing: the line joining the points $P_1(x_1, y_1)$ and $P_2(x_2, y_2)$ has slope $\frac{y_2 - y_1}{x_2 - x_1}$.

Example: $A(3, -1)$, $B(-2, 4)$

$$\text{Slope of } \overline{AB} = \frac{4 - (-1)}{-2 - 3} = \frac{5}{-5} = -1$$

11 to 15: Find the slope of the line joining the given points:

11. $(-3, 1)$ and $(-1, -4)$
 12. $(0, 2)$ and $(-3, -5)$
 13. $(3, -1)$ and $(5, -1)$

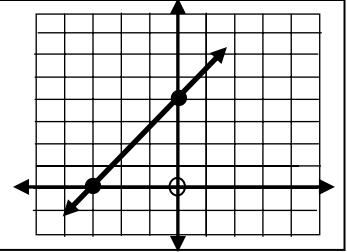


To find the x -intercept (x -axis crossing) of an equation, let y be zero and solve for x . For the y -intercept, let x be zero and solve for y .

Example: $3y - 4x = 12$

If $x = 0$, $y = 4$ so the y -intercept is 4.

If $y = 0$, $x = -3$ so the x -intercept is -3 .

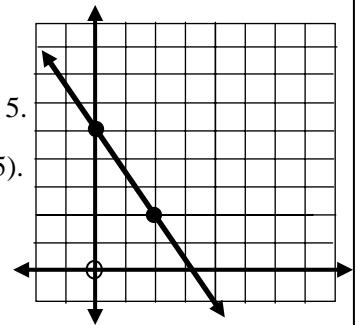


The graph of $y = mx + b$ is a line with slope m and y -intercept b . To draw the graph, find one point on it [such as $(0, b)$] and then use the slope to find another point. Draw the line joining the two.

Example: $y = \frac{-3}{2}x + 5$

has slope $-\frac{3}{2}$ and y -intercept 5.

To graph the line, locate $(0, 5)$. From that point, go down 3 (top of slope fraction), and over (right) 2 (bottom of fraction) to find a second point. Join.



16 to 20: Find slope and y -intercept, and sketch the graph:

16. $y = x + 4$

19. $x - y = -1$

17. $y = -\frac{1}{2}x - 3$

20. $x = -3y + 2$

18. $2y = 4x - 8$

To find an equation of a non-vertical line, it is necessary to know its slope and one of its points. Write the slope of the line thru (x, y) and the known point, then write an equation which says that this slope equals the known slope.

Example: Find an equation of the line thru $(-4, 1)$ and $(-2, 0)$.

$$\text{Slope} = \frac{1 - 0}{-4 - (-2)} = \frac{1}{-2}$$

Using $(-2, 0)$ and (x, y) , slope = $\frac{y - 0}{x - (-2)} = \frac{1}{-2}$;

cross-multiply, get $-2y = x + 2$, or $y = -\frac{1}{2}x - 1$

21 to 25: Find an equation of the line:

21. thru $(-3, 1)$ and $(-1, -4)$

22. thru $(0, -2)$ and $(-3, -5)$

23. thru $(3, -1)$ and $(5, -1)$

24. thru $(8, 0)$, with slope -1

25. thru $(0, -5)$, with slope $2/3$

Practice Problems for Transfer Math Readiness Questions – Topic 6: Graphing and the Coordinate Plane

A vertical line has no slope, and its equation can be written so it looks like $x = k$ (where k is a number). A horizontal line has zero slope, and its equation looks like $y = k$.

Example: Graph on the same graph:
 $x - 3 = 1$ and $1 + y = -3$.

The first equation is $x = 4$.

The second is $y = -4$.

26 to 27: Graph and write equations for:

26. the line thru $(-1, 4)$ and $(-1, 2)$.
27. the horizontal line thru $(4, -1)$.

D. Linear Inequalities in Two Variables:

Example: Two variable graph: graph solution on number plane: $x - y > 3$.

(This is an abbreviation for $\{(x,y):x - y > 3\}$. Subtract x , multiply by -1 , get $y < x - 3$.

Graph $y = x - 3$, but draw a dotted line, and shade the side where $y < x - 3$.

28 to 33: Graph:

- | | |
|-------------------------------|------------------|
| 28. $y < 3$ | 31. $x < y + 1$ |
| 29. $y > x$ | 32. $x + y < 3$ |
| 30. $y \geq \frac{2}{3}x + 2$ | 33. $2x - y > 1$ |

E. Graphing Quadratic Equations: The graph of $y = ax^2 + bx + c$ is a parabola, opening upward (if $a > 0$) or downward (if $a < 0$), and with line of symmetry $x = \frac{-b}{2a}$, also called axis of symmetry.

To find the vertex $V(h, k)$ of the parabola, $h = \frac{-b}{2a}$ (since V is on the axis of symmetry), and k is the value of y when h is substituted for x .

Examples:

1) $y = x^2 - 6x$
 $a = 1, b = -6, c = 0$
 Axis: $x = \frac{-b}{2a} = \frac{6}{2} = 3$
 $h = 3, k = 3^2 - 18 = -9$
 Thus, vertex is $(3, -9)$

2) $y = 3 - x^2; V(0, 3)$,
 Axis: $x = 0$
 y-intercept: if $x = 0, y = 3 - 0^2 = 3$
 x-intercept: if $y = 0, 0 = 3 - x^2$ so, $3 = x^2$,
 And $x = \pm\sqrt{3}$

34 to 40: Sketch the graph:

- | | |
|-------------------|--------------------------|
| 34. $y = x^2$ | 38. $y = (x + 1)^2$ |
| 35. $y = -x^2$ | 39. $y = (x - 2)^2 - 1$ |
| 36. $y = x^2 + 1$ | 40. $y = (x + 2)(x - 1)$ |
| 37. $y = x^2 - 3$ | |

Answers:

- 1.
2. IV
3. x
4. y
5. y
6. x
7. 5
8. 3
9. $\sqrt{29}$
10. 7
11. $-5/2$
12. $7/3$
13. 0
14. $-3/5$
15. $3/4$
16. $m = 1$
 $b = 4$
17. $m = -1/2$
 $b = -3$
18. $m = 2$
 $b = -4$
19. $m = 1$
 $b = 1$
20. $m = -1/3$
 $b = 2/3$

21. $y = -5/2x - 13/2$
22. $y = x - 2$
23. $y = -1$
24. $y = -x + 8$
25. $y = 2/3x - 5$
26. $x = -1$
27. $y = -1$
- 28.
- 29.
- 30.

- 31.
- 32.
- 33.
- 34.
- 35.
- 36.
- 37.
- 38.
- 39.
- 40.

Practice Problems for Transfer Math Readiness Questions – Topic 7: Logarithms and Functions

Directions: Study the examples, work the problems, then check your answers on the back of this sheet. If you don't get the answer given, check your work and look for mistakes. If you have trouble, ask a math teacher or someone else who understands this topic.

A. **Functions:** The area A of a square depends on its side length s , and we say A is a function of s , and write ' $A = f(s)$ '; for short, we read this ' $A = f$ of s '. There are many functions of s . The one here is s^2 . We write this $f(s) = s^2$ and can translate: 'the function of s we're talking about is s^2 '. Sometimes we write $A(s) = s^2$. This says the area A is a function of s , and specifically, it is s^2 .

B. **Function Values and Substitution:** If $A(s) = s^2$, $A(3)$, read 'A of 3', means replace every s in $A(s) = s^2$ with 3, and find A when s is 3. When we do this, we find $A(3) = 3^2 = 9$.

Examples: $g(x)$ is given: $y = g(x) = \pi x^2$

- 1) $g(3) = \pi \cdot 3^2 = 9\pi$
- 2) $g(7) = \pi \cdot 7^2 = 49\pi$
- 3) $g(a) = \pi a^2$
- 4) $g(x + h) = \pi \cdot (x + h)^2 = \pi x^2 + 2\pi xh + \pi h^2$

1. Given $y = f(x) = 3x - 2$. Complete these ordered pairs:
 $(3, \underline{\quad})$, $(0, \underline{\quad})$, $(1/2, \underline{\quad})$,
 $(\underline{\quad}, 10)$, $(\underline{\quad}, -1)$, $(x - 1, \underline{\quad})$

2 to 10: Given $f(x) = x^2 - 4x + 2$. Find:

- | | |
|--------------|-----------------|
| 2. $f(0) =$ | 7. $f(x) - 2 =$ |
| 3. $f(1) =$ | 8. $f(x - 2) =$ |
| 4. $f(-1) =$ | 9. $2f(x) =$ |
| 5. $f(-x) =$ | 10. $f(2x) =$ |
| 6. $-f(x) =$ | |

11 to 15: Given $f(x) = \frac{x}{x+1}$. Find:

- | | |
|---------------|------------------|
| 11. $f(1) =$ | |
| 12. $f(-2) =$ | 14. $f(-1) =$ |
| 13. $f(0) =$ | 15. $f(x - 1) =$ |

Example: If $k(x) = x^2 - 4x$, for what x is $k(x) = 0$?

If $k(x) = 0$, then $x^2 - 4x = 0$ and since $x^2 - 4x = x(x - 4) = 0$, x can be either 0 or 4. (These values of x : 0 and 4, are called 'zeros of the function', because each makes the function zero.)

16 to 19: Find all real zeros of:

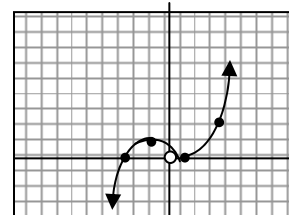
- | | |
|--------------------|----------------------|
| 16. $x(x + 1)$ | 18. $x^2 - 16x + 64$ |
| 17. $2x^2 - x - 3$ | 19. $x^2 + x + 2$ |

20 to 23: Given: $f(x) = x^2 - 4x + 2$, find real x so that:

- | | |
|-----------------|-----------------------------|
| 20. $f(x) = -2$ | 22. $f(x) = -3$ |
| 21. $f(x) = 2$ | 23. x is a zero of $f(x)$ |

Since $y = f(x)$, the values of y are the values of the function which correspond to specific values of x . The heights of the graph above (or below) the x -axis are the values of y and so also of the function.

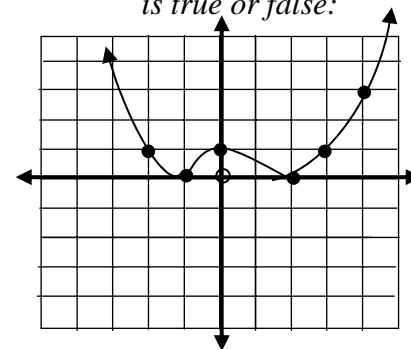
Thus for this graph, $f(3)$ is the height (value) of the function at $x = 3$ and the value is 2: At $x = -3$, the value (height) of $f(x)$ is zero; in other words, $f(-3) = 0$.



Note that $f(3) > f(-3)$, since $2 > 0$, and that $f(0) < f(-1)$, since $f(-1) = 1$ and $f(0) < 1$.

24 to 28: For this graph, tell whether the statement is true or false:

24. $g(-1) = g(0)$
25. $g(0) = g(3)$
26. $g(1) > g(-1)$
27. $g(-2) > g(1)$
28. $g(2) < g(0) < g(4)$



C. **Logarithms and Exponents:**

Exponential form: $2^3 = 8$

Logarithmic form: $\log_2 8 = 3$

Both of the equations above say the same thing. ' $\log_2 8 = 3$ ' is read 'log base two of eight equals three' and translates 'the power of 2 which gives 8 is 3'.

29 to 32: Write the following information in both exponential and logarithmic forms:

29. The power of 3 which gives 9 is 2.
30. The power of x which gives x^3 is 3.
31. 10 to the power -2 is $\frac{1}{100}$.
32. $\frac{1}{2}$ is the power of 169 which gives 13.

33 to 38: Write in logarithmic form:

- | | |
|----------------|------------------------------|
| 33. $4^3 = 64$ | 36. $\frac{1}{10} = 10^{-1}$ |
| 34. $3^0 = 1$ | 37. $a^b = c$ |
| 35. $25 = 5^2$ | 38. $y = 3^x$ |

Practice Problems for Transfer Math Readiness Questions – Topic 7: Logarithms and Functions

39 to 44: Write in exponential form:

39. $\log_3 9 = 2$ 42. $1 = \log_4 4$
 40. $\log_3 1 = 0$ 43. $y = \log_a x$
 41. $5 = \log_2 32$ 44. $\log_b a = 2$

45 to 50: Find the value:

45. $2^{10} =$ 48. $\frac{6^{10}}{3^{10}} =$
 46. $\log_4 4^{10} =$ 49. $\log_{49} 7 =$
 47. $\log_6 6 =$ 50. $\log_7 49 =$

D. Logarithm and Exponent Rules:

<p>Exponent Rules: (all quantities real)</p> $a^b \cdot a^c = a^{b+c}$ $\frac{a^b}{a^c} = a^{b-c}$ $\frac{a^c}{a^c} = a^{bc}$ $(a^b)^c = a^{bc}$ $(ab)^c = a^c \cdot b^c$ $\left(\frac{a}{b}\right)^c = \frac{a^c}{b^c}$ $a^0 = 1$, (if $a \neq 0$) $a^{-b} = \frac{1}{a^b}$ $a^{\frac{p}{r}} = \sqrt[r]{a^p} = (\sqrt[r]{a})^p$	<p>Log Rules: (base any positive real # except 1)</p> $\log ab = \log a + \log b$ $\log \frac{a}{b} = \log a - \log b$ $\log a^b = b \log a$ $\log_a a^b = b$ $a(\log_a b) = b$ $\log_a b = \frac{\log_c b}{\log_c a}$ (base change rule) (think of $\frac{p}{r}$ as $\frac{\text{power}}{\text{root}}$)
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51 to 52: Given $\log_2 1024 = 10$, find:

51. $\log_2 1024^5 =$ 52. $\log_2 \sqrt{1024} =$

53 to 63: Solve for x in terms of y and z :

53. $3^x = 3^y \cdot 3^z$ 57. $\log x^2 = 3 \log y$
 54. $9^y = \frac{3^z}{3^x}$ 56. $\log x = 2 \log y - \log z$
 55. $x^3 = y$ 58. $3 \log x = \log y$
 56. $3^x = y$ 60. $\log x = \log y + \log z$
 61. $\log \sqrt{x} + \log \sqrt[3]{y} = \log z^2$
 62. $\log_7 3 = y$; $\log_7 2 = z$; $x = \log_3 2$
 63. $y = \log_a 9$; $x = \log_a 3$

E. Logarithmic and Exponential Equations:

64 to 93: Use the exponent and log rules to find the value of x :

64. $6^{2x} = 6^3$ 70. $4^3 \cdot 4^5 = 4^x$
 65. $2^{2x} = 2^3$ 71. $3^{-2} = x$
 66. $4^x = 8$ 72. $\frac{3^x}{3} = 3^0$
 67. $9^x = 27^{x-1}$ 73. $(5^2)^3 = 5^x$
 68. $\log_3 x = \log_3 6$ 74. $5^{x+1} = 1$
 69. $\log_3 4x = \log_3 6$ 75. $\log_3 3^7 = x$
 76. $6^{(\log_6 x)} = 8$
 77. $\log_{10} x = \log_{10} 4 + \log_{10} 2$
 78. $\log_3 2x = \log_3 8 + \log_3 4 - 4 \log_3 2$
 79. $\log_x 25 = 2$
 80. $3 \log_a 4 = \log_a x$

81. $\log(2x - 6) = \log(6 - x)$

82. $\frac{\log_x 3}{\log_x 4} = \log_4 3$

83. $\log_3(27 \cdot 3^{-4}) = x$

84. $\frac{\log_3 81}{\log_3 27} = \log_3 \frac{81}{27} = x$

85. $\log_4 \sqrt[3]{30} = x$ $\log_4 30$

86. $\log_2 \frac{1}{32} = x$

87. $\log_{16} x = \frac{3}{2}$

88. $\log_4 64 = x$

89. $\sqrt[4]{5} = 5^x$

90. $27^x = \left(\frac{1}{9}\right)^3$

91. $4^{10} = 2^x$

92. $2^x = 3$

93. $3 \cdot 2^x = 4$

Answers:

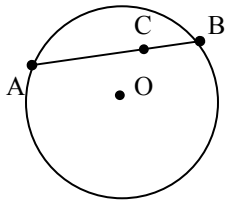
- | | |
|------------------------------------|--------------------------------------|
| 1. 7, -2, -1/2, 4, | 53. $y + z$ |
| 1/3, $3x - 5$ | 54. $z - 2y$ |
| 2. 2 | 55. $y^{1/3} = \sqrt[3]{y}$ |
| 3. -1 | 56. $\log_3 y$ |
| 4. 7 | 57. $y^{3/2} = y\sqrt{y}$ |
| 5. $x^2 + 4x + 2$ | 58. $\frac{y^2}{z}$ |
| 6. $-x^2 + 4x + 2$ | 59. $\sqrt[3]{y}$ |
| 7. $x^2 - 4x$ | 60. $\frac{yz}{z^4}$ |
| 8. $x^2 - 6x + 14$ | 61. $\sqrt[3]{y^2}$ |
| 9. $2x^2 - 8x + 4$ | 62. z/y |
| 10. $4x^2 + 8x + 2$ | 63. $y/2$ |
| 11. 1/2 | 64. 3/2 |
| 12. 2 | 65. 3/2 |
| 13. 0 | 66. 3/2 |
| 14. no value | 67. 3 |
| 15. $\frac{x-1}{x}$ | 68. 6 |
| 16. -1, 0 | 69. 3/2 |
| 17. -1, 3/2 | 70. 8 |
| 18. 8 | 71. 1/9 |
| 19. none | 72. 1 |
| 20. 2 | 73. 6 |
| 21. 0, 4 | 74. -1 |
| 22. none | 75. 7 |
| 23. $2 \pm \sqrt{2}$ | 76. 8 |
| 24. P | 77. 8 |
| 25. T | 78. 1 |
| 26. T | 79. 5 |
| 27. T | 80. 64 |
| 28. T | 81. 4 |
| 29. $3^2 = 9$; $\log_3 9 = 2$ | 82. any real number |
| 30. $x^3 = x^3$; $\log_x x^3 = 3$ | > 0 and $\neq 1$ |
| 31. $10^{-2} = 1/100$; | 83. -1 |
| $\log_{10} 1/100 = -2$ | 84. 1/3 |
| 32. $169^{1/2} = 13$; | 85. 1/3 |
| $\log_{169} 13 = 1/2$ | 86. -5 |
| 33. $\log_4 64 = 3$ | 87. 64 |
| 34. $\log_3 1 = 0$ | 88. 3 |
| 35. $\log_5 25 = 2$ | 89. 1/4 |
| 36. $\log_{10} 1/10 = -1$ | 90. -2 |
| 37. $\log_a c = b$ | 91. 20 |
| 38. $\log_3 y = x$ | 92. $\frac{\log 3}{\log 2}$ |
| 39. $3^2 = 9$ | 93. $\frac{\log 4 - \log 3}{\log 2}$ |
| 40. $3^0 = 1$ | (any base; |
| 41. $2^5 = 32$ | if base = 2, |
| 42. $4^1 = 4$ | $x = 2 - \log_2 3$) |
| 43. $a^y = x$ | |
| 44. $b^2 = a$ | |
| 45. 1024 | |
| 46. 10 | |
| 47. 1 | |
| 48. $2^{10} = 1024$ | |
| 49. 1/2 | |
| 50. 2 | |
| 51. 50 | |
| 52. 5 | |

Practice Problems for Transfer Math Readiness Questions – Topic 8: Word Problems

Directions: Study the examples, work the problems, then check your answers on the back of this sheet. If you don't get the answer given, check your work and look for mistakes. If you have trouble, ask a math teacher or someone else who understands this topic.

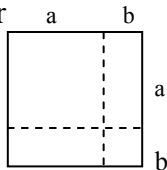
- $\frac{2}{3}$ of $\frac{1}{6}$ of $\frac{3}{4}$ of a number is 12. What is the number?
- On the number line, points P and Q are 2 units apart. Q has coordinate x . What are the possible coordinates of P ?
- What is the number, which when multiplied by 32, gives $32 \cdot 46$?
- If you square a certain number, you get 9^2 . What is the number?
- What is the power of 36 that gives you $36^{1/2}$?
- Point X is on each of two given intersecting lines. How many such points X are there?
- Point Y is on each of two given circles. How many such points Y are there?
- Point Z is on each of a given circle and a given ellipse. How many such Z are there?
- Point R is on the coordinate plane so its distance from a given point A is less than 4. Show in a sketch where R could be.

10 to 11:

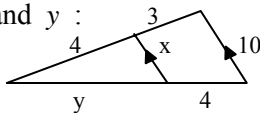


- If the length of chord AB is x and the length of CB is 16, what is AC ?
- If $AC = y$ and $CB = z$, How long is AB (in terms of y and z)?

- This square is cut into two smaller squares and two non-square rectangles as shown. Before being cut, the large square had area $(a + b)^2$. The two smaller squares have areas a^2 and b^2 . Find the total area of the two non-square rectangles. Do the areas of the 4 parts add up to the area of the original square?



- Find x and y :



- In order to construct an equilateral triangle with an area which is 100 times the area of a given equilateral triangle, how long a side should be used?

15 to 16: x and y are numbers, and two x 's equals three y 's.

- Which of x or y must be larger?
- What is the ratio of x to y ?

17 to 21: A plane has a certain speed in still air. In still air, it goes 1350 miles in 3 hours.

- What is its (still air) speed?
- How long does it take to fly 2000 mi.?
- How far does the plane go in x hours?
- If the plane flies against a 50 mph headwind, what is its ground speed?
- If it has fuel for 7.5 hours of flying time, how far can it go against this headwind?

22 to 32: Georgie and Porgie bake pies. Georgie can complete 30 pies an hour.

- How many can he make in one minute?
- How many can he make in 10 minutes?
- How many can he make in x minutes?
- How long does he take to make 200 pies?

26 to 28: Porgie can finish 45 pies an hour.

- How many can she make in one minute?
- How many can she make in 20 minutes?
- How many can she make in x minutes?

29 to 32: If they work together, how many pies can they produce in:

- | | |
|-----------------|----------------|
| 29. 1 minute | 31. 80 minutes |
| 30. x minutes | 32. 3 hours |

33 to 41: A nurse needs to mix some alcohol solutions, given as a percent by weight of alcohol in water. Thus in a 3% solution, 3% of the weight would be alcohol. She mixes x gm of 3% solution, y gm of 10% solution, and 10 gm of pure water to get a total of 140 gm of a solution which is 8% alcohol.

- In terms of x , how many gm of alcohol are in the 3% solution?
- The y gm of 10% solution would include how many gm of alcohol?
- How many gm of solution are in the final mix (the 8% solution)?
- Write an expression in terms of x and y for the total number of gm in the 8% solution contributed by the three ingredients (the 3%, 10% and water).
- Use your last two answers to write a 'total grams equation'.
- How many gm of alcohol are in the 8%?
- Write an expression in terms of x and y for the total number of gm of alcohol in the final solution.
- Use the last two answers to write a 'total grams of alcohol equation'.
- How many gm of each solution are needed?

Practice Problems for Transfer Math Readiness Questions – Topic 8: Word Problems

42. Half the square of a number is 18. What is the number?
43. If the square of twice a number is 81, what is the number?
44. Given a positive number x . The square of a positive number y is at least four times x . How small can y be?
45. Twice the square of half of a number is x . What is the number?

- 46 to 48: *Half of x is the same as one-third of y .*
46. Which of x and y is the larger?
47. Write the ratio $x:y$ as the ratio of two integers.
48. How many x 's equal 30 y 's?

- 49 to 50: *A gathering has twice as many women as men. W is the number of women and M is the number of men.*
49. Which is correct: $2M = W$ or $M = 2W$?
50. If there are 12 women, how many men are there?

- 51 to 53: *If A is increased by 25%, it equals B .*
51. Which is larger, B or the original A ?
52. B is what percent of A ?
53. A is what percent of B ?

- 54 to 56: *If C is decreased by 40%, it equals D .*
54. Which is larger, D or the original C ?
55. C is what percent of D ?
56. D is what percent of C ?

- 57 to 58: *The length of a rectangle is increased by 25% and its width is decreased by 40%.*
57. Its new area is what percent of its old area?
58. By what percent has the old area increased or decreased?

- 59 to 61: *Your wage is increased by 20%, then the new amount is cut by 20% (of the new amount).*
59. Will this result in a wage which is higher than, lower than, or the same as the original wage?
60. What percent of the original wage is this final wage?
61. If the above steps were reversed (20% cut followed by 20% increase), the final wage would be what percent of the original wage?

62. Find 3% of 36.
63. 55 is what percent of 88?
64. What percent of 55 is 88?
65. 45 is 3% of what number?
66. The 3200 people who vote in an election are 40% of the people registered to vote. How many are registered?
67. If you get 36 on a 40-question test, what percent is this?
68. What is the average of 87, 36, 48, 59, and 95?
69. If two test scores are 85 and 60, what minimum score on the next test would be needed for an overall average of 80?
70. The average height of 49 people is 68 inches. What is the new average height if a 78-inch person joins the group?

71 to 72: s varies directly as P , and $P = 56$ when $s = 14$.


71. Find s when $P = 144$.
72. Find P when $s = 144$.

73 to 74: A is proportional to r^2 , and when $r = 10$, $A = 400\pi$.

73. Find A when $r = 15$.
74. Find r when $A = 36\pi$.

75. If b is inversely proportional to h , and $b = 36$ when $h = 12$, find h when $b = 3$.
76. If $3x = 4y$, write the ratio $x:y$ as the ratio of two integers.
77. The length of a rectangle is twice the width. If both dimensions are increased by 2 cm, the resulting rectangle has 84 cm^2 . What was the original width?
78. After a rectangular piece of knitted fabric shrinks in length one cm and stretches in width 2 cm, it is a square. If the original area was 40 cm^2 , what is the square area?

Answers:

- | | |
|---|---------------------------|
| 1. 144 | 39. $0.03x + .01y$ |
| 2. $x + 2, x - 2$ | 40. $0.03x + 0.1y = 11.2$ |
| 3. 46 | 41. $x = 180/7$ |
| 4. 9 | $y = 730/7$ |
| 5. $1/2$ | 42. 6, -6 |
| 6. 1 | 43. $4.5, -4.5$ |
| 7. 0, 1, or 2 | 44. $2\sqrt{x}$ |
| 8. 0, 1, 2, 3, or 4 | 45. $\sqrt{2x}$ |
| 9.  Inside the circle of radius 4 centered on A | 46. y |
| 10. $x - 16$ | 47. $2/3$ |
| 11. $y + x$ | 48. 45 |
| 12. $2ab$, yes: $(a + b)^2 = a^2 + 2ab + b^2$ | 49. $2M = W$ |
| 13. $x = 40/7$ | 50. 6 |
| $y = 16/3$ | 51. 8 |
| 14. 10 times the original side | 52. 125% |
| 15. x | 53. 80% |
| 16. $3/2$ | 54. C |
| 17. 450 mph | 55. $166 \frac{2}{3} \%$ |
| 18. $4 \frac{4}{9}$ hrs. | 56. 60% |
| 19. $450x$ miles | 57. 75% |
| 20. 400 mph | 58. 25% decrease |
| 21. 3000 miles | 59. lower |
| 22. $1/2$ | 60. 96% |
| 23. 5 | 61. same (96%) |
| 24. $x/2$ | 62. 1.08 |
| 25. 400 min. | 63. 62.5% |
| 26. $3/4$ | 64. 160% |
| 27. 15 | 65. 1500 |
| 28. $3x/4$ | 66. 8000 |
| 29. $5/4$ | 67. 90% |
| 30. $5x/4$ | 68. 65 |
| 31. 100 | 69. 95 |
| 32. 225 | 70. 68.2 in. |
| 33. $0.03x$ | 71. 36 |
| 34. $0.1y$ | 72. 576 |
| 35. 140 | 73. 900π |
| 36. $x + y + 10$ | 74. 3 |
| 37. $x + y + 10 = 140$ | 75. 144 |
| 38. 11.2 | 76. 4:3 |
| | 77. 5 |
| | 78. 49 |